

Optical Remote Sensing

Basic Physics

- Radiometry
- Reflectance

Martin.Bachmann@dlr.de & Rudolf.Richter@dlr.de

1. Radiometry

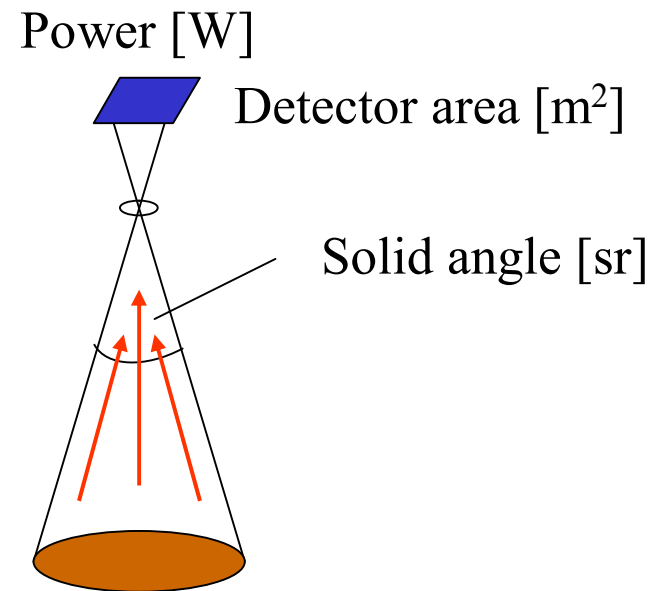
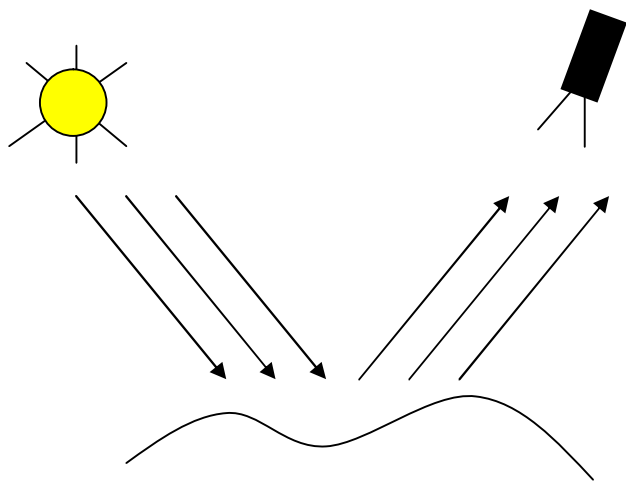
Basic Definitions

- **Radiant Energy** Q [J] = [W s]
- **Radiant Power**, or: photon flux Φ [W] = dQ/dt
i.e. Energy per time interval
- **Radiant Flux** F [W m⁻²]
E: irradiance // M: emittance (thermal sources)
i.e. Power per area
sun: irradiance is flux perpendicular to propagation (directional flux)
general term of flux: includes hemispherical radiation
- **Radiant Intensity** I [W sr⁻¹]
i.e. Power per solid angle
- **Radiance** L [W m⁻² sr⁻¹]
i.e. Power per (detector) area and solid angle
- **Spectral quantities, e.g. spectral radiance: L per bandwidth:**
 L_λ [W m⁻² sr⁻¹ μm]

- The sensor detects:

Radiance, At-Sensor Radiance L [$\text{W m}^{-2} \text{sr}^{-1}$] or [$\text{W m}^{-2} \text{sr}^{-1} \mu\text{m}$]

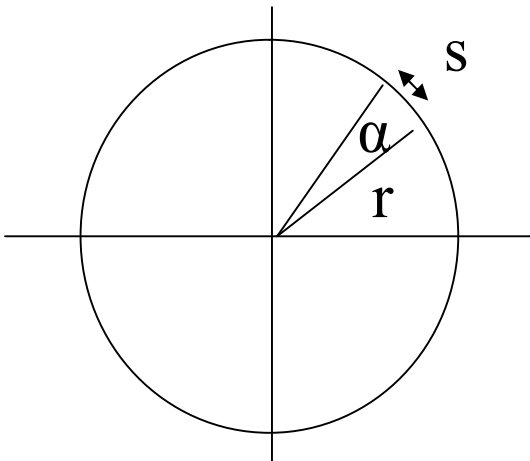
=> Unit after system correction, described as L1 product



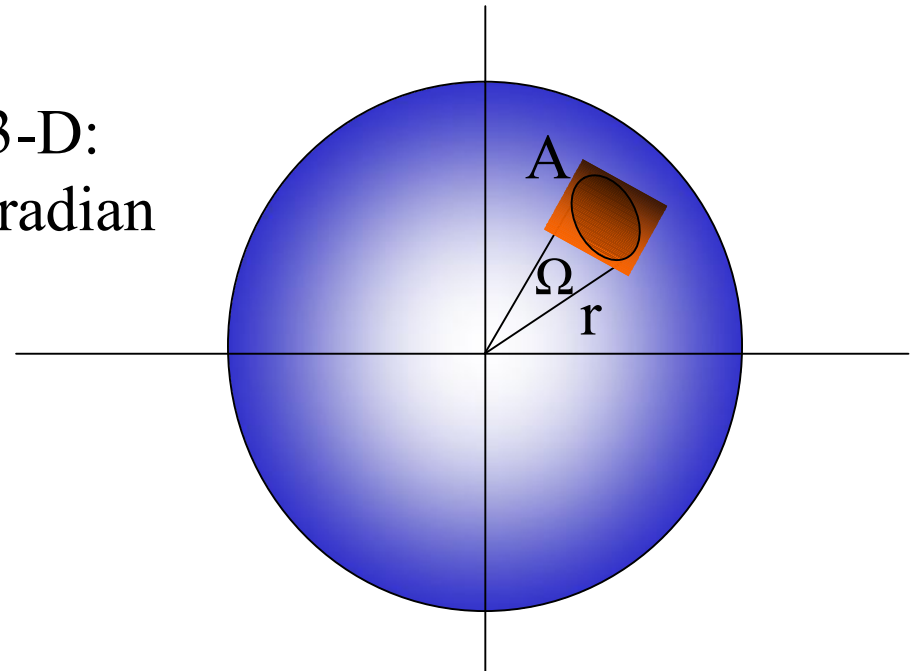
Physical Basics

- Solid Angle Ω steradian = area / radius²
- Sphere = $4\pi r^2 / r^2 = 4\pi$ [sr]
- Sky = 2π [sr]

In 2-D:
Radian



In 3-D:
Steradian



Physical Basics

Spectral Response $R(\lambda)$: relative or normalized: 0 - 1

absolute: $R_{abs} = c R_{norm}$

meas.: $L = \int R_{abs}(\lambda) L(\lambda) d\lambda \quad (W m^{-2} sr^{-1})$

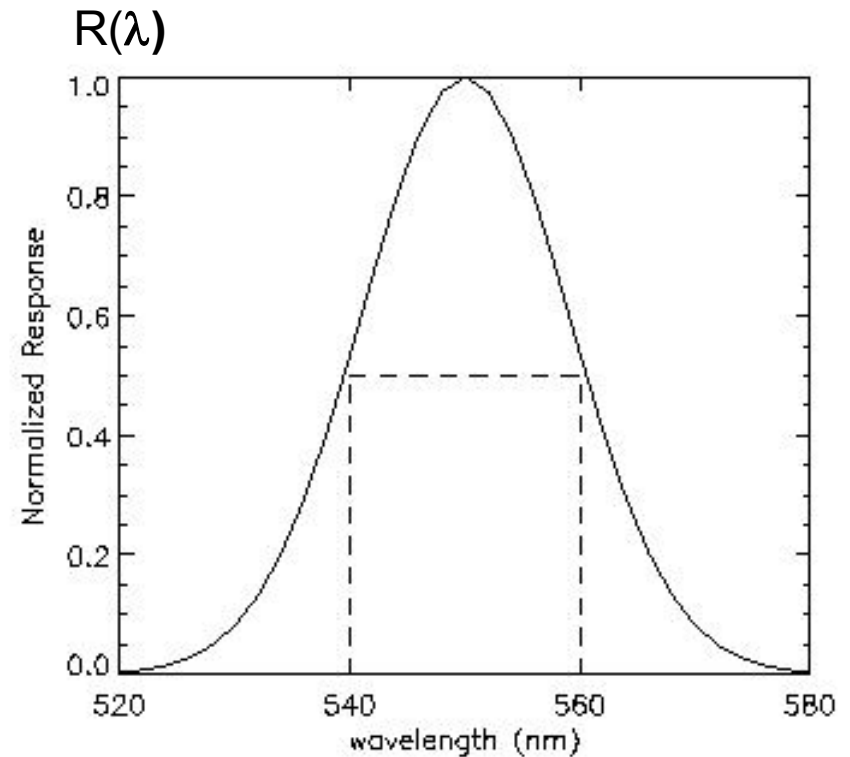
normalized:

$$L_{\Delta\lambda} = \frac{\int R(\lambda) L(\lambda) d\lambda}{\int R(\lambda) d\lambda} \quad (W m^{-2} sr^{-1} nm^{-1})$$

Advantage of normalized radiance :
nearly independent of $R(\lambda)$

Normalized is sufficient in most cases:

$$\rho = \frac{\pi L_{abs}}{E_{abs}} = \frac{\pi c L_{norm}}{c E_{norm}} = \frac{\pi L_{\Delta\lambda}}{E_{\Delta\lambda}}$$



Spectral Resolution (bandwidth):

(full width at half max FWHM, $\Delta\lambda$)

Nomenclature: $L, L(\lambda), L_\lambda, L_{\Delta\lambda}$ Pay attention to unit!

Physical Basics

- Planck:

$$\text{Emittance } M = f(\lambda, T)$$

- Boltzmann:

$$M_{\text{blackbody}} = \sigma T^4 \text{ [W m}^{-2}\text{]}$$

$$\sigma = 5.67 * 10^{-8} \text{ W m}^{-2} \text{ K}^{-1}$$

In general: $M = \varepsilon(\lambda) T^n$

n...property of material, ~4

- Wien:

The higher the temperature (T) the shorter the wavelength (λ_{max}) of maximal energy emittance

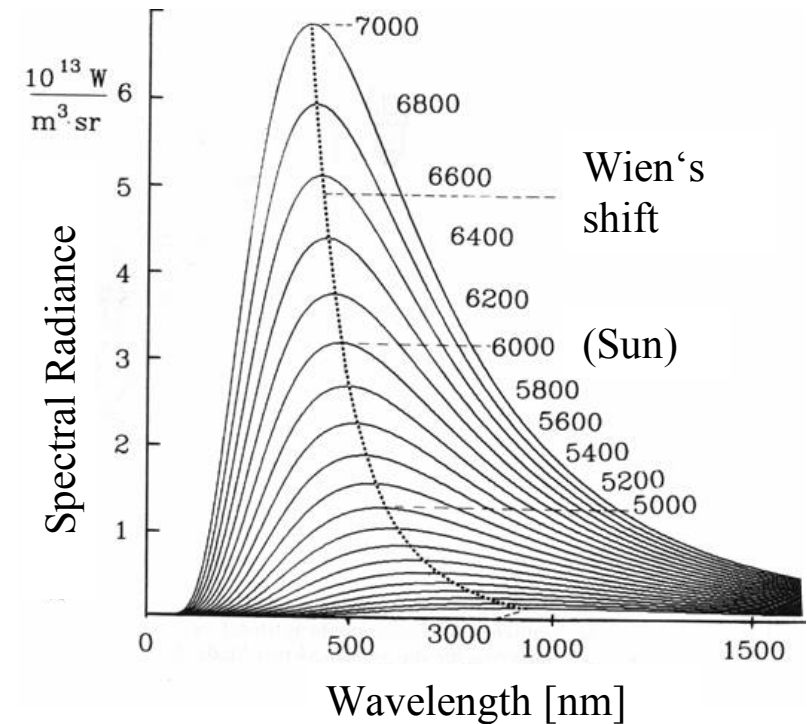
$$\lambda_{\text{max}} = 2898 / T$$

Physical Basics

- Electromagnetic wave (Maxwells Equation)
- Electric vector perpendicular to magnetic
- $c = \lambda * \nu$ $c \dots$ Lightspeed in vacuum $3 * 10^8 \text{ m s}^{-1}$
 $\nu \dots$ Frequency

- Energy $q = h * \nu$
 h : Planck's Constant: $6.63 * 10^{-34} \text{ [J s]}$
 → Higher energy per photon with shorter wavelength

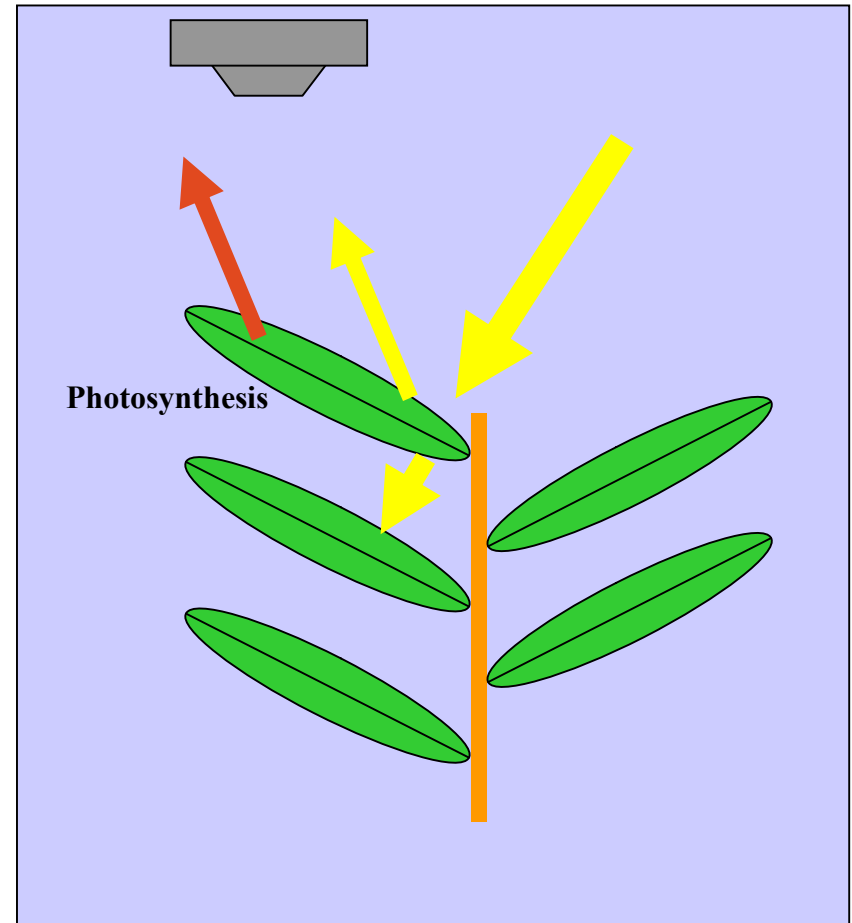
- Energy per Photon: green $0.55 \text{ }\mu\text{m}$ **→** $3.61 * 10^{-19} \text{ J}$
 TIR $12 \text{ }\mu\text{m}$ **→** $1.66 * 10^{-20} \text{ J}$
 → 22times higher energy!



2: Interaction with Matter

Physical basics

- Absorption (uptake of energy)
 - Electron transfer, rotation, vibration
 - Heating, change in matter, emission
- Emission („release“ of energy)
 - Electron transfer, rotation, vibration
- Reflection
 - Change of direction without energy uptake
- Transmission
 - Transfer without absorption or reflection



Physical basics

Energy balance relationship:

- $E_{\text{emitted by sun}} = E_{\text{reflected}} + E_{\text{transmitted}} + E_{\text{absorbed}}$

E... Incident Energy [W]

- $1 = E_r / E_i + E_t / E_i + E_a / E_i$

- $1 = R + T + A$

...Reflection-coefficient + Transmission-coefficient + Absorption-coefficient

- opaque material: $T = 0 \rightarrow 1 = R + A$

=> Material property, independent of incoming radiant energy!

Absorption

- Sounds pretty simple, **but**:
 - Some features are related to many materials:
e.g. OH bond is related to water, cellulose, starch, clays etc.
 - Overlapping features
 - Multiple scattering broadens features
 - No simple relationship between feature depth and component content
(saturation effects)
 - In Vivo \neq In Vitro
 - Noise, spectral bandwidth and position, ...

3: Reflectance Behavior

Physical basics

Reflection behaviour of surfaces

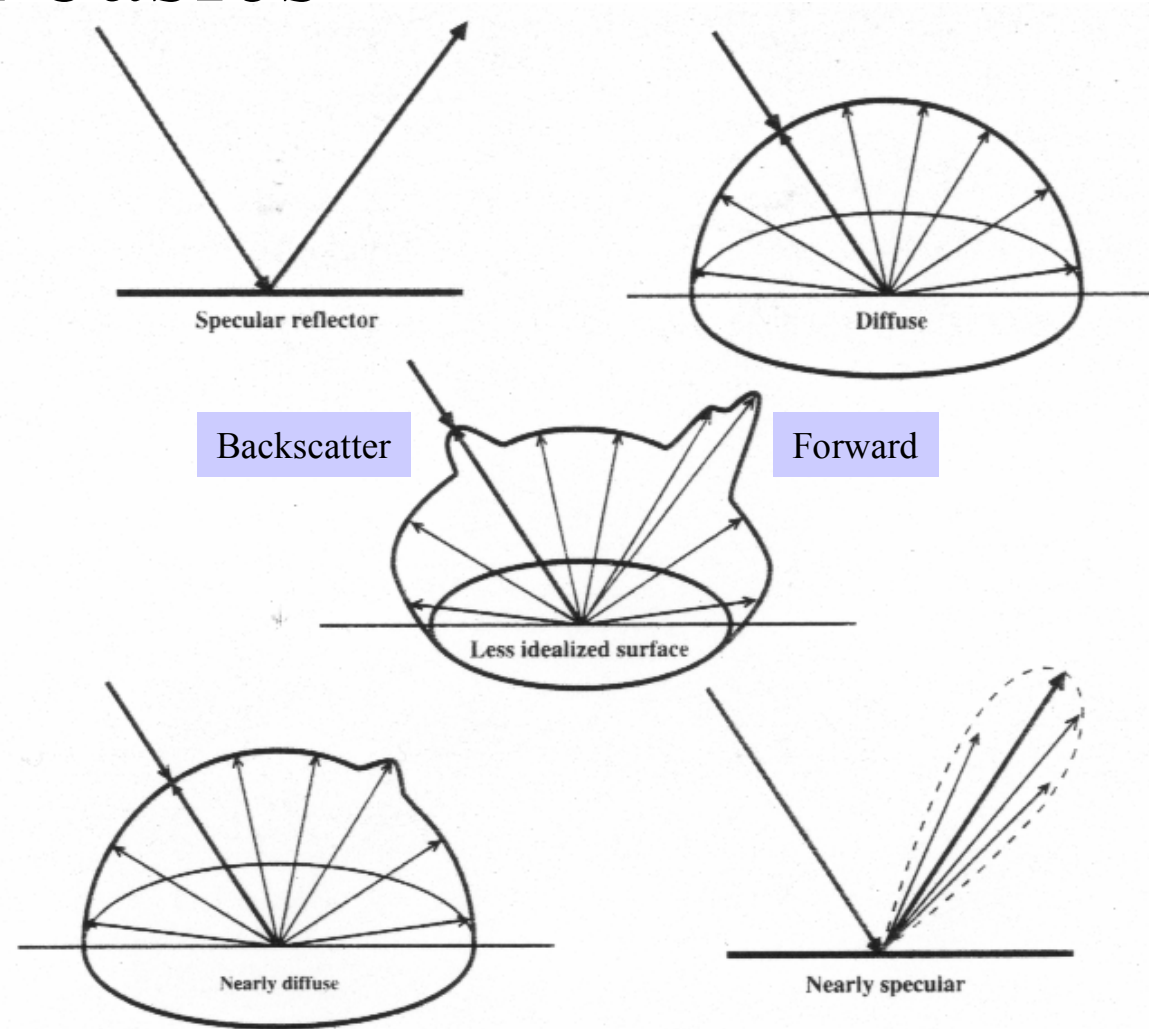
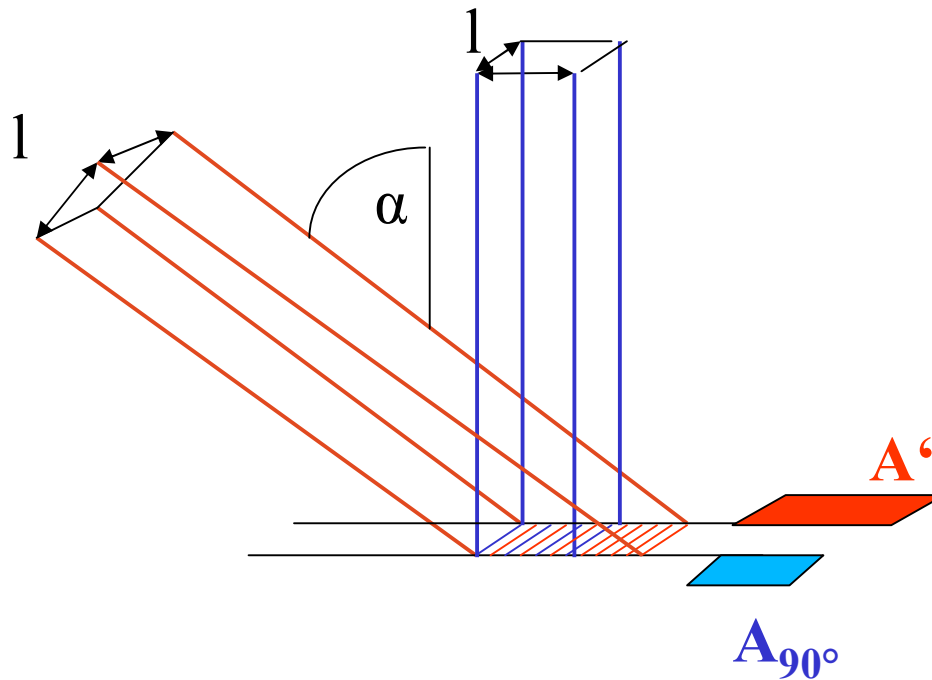


Figure 4.7 Reflectance characteristics of idealized surfaces.

Physical Basics

Lambertian Cos.-Law



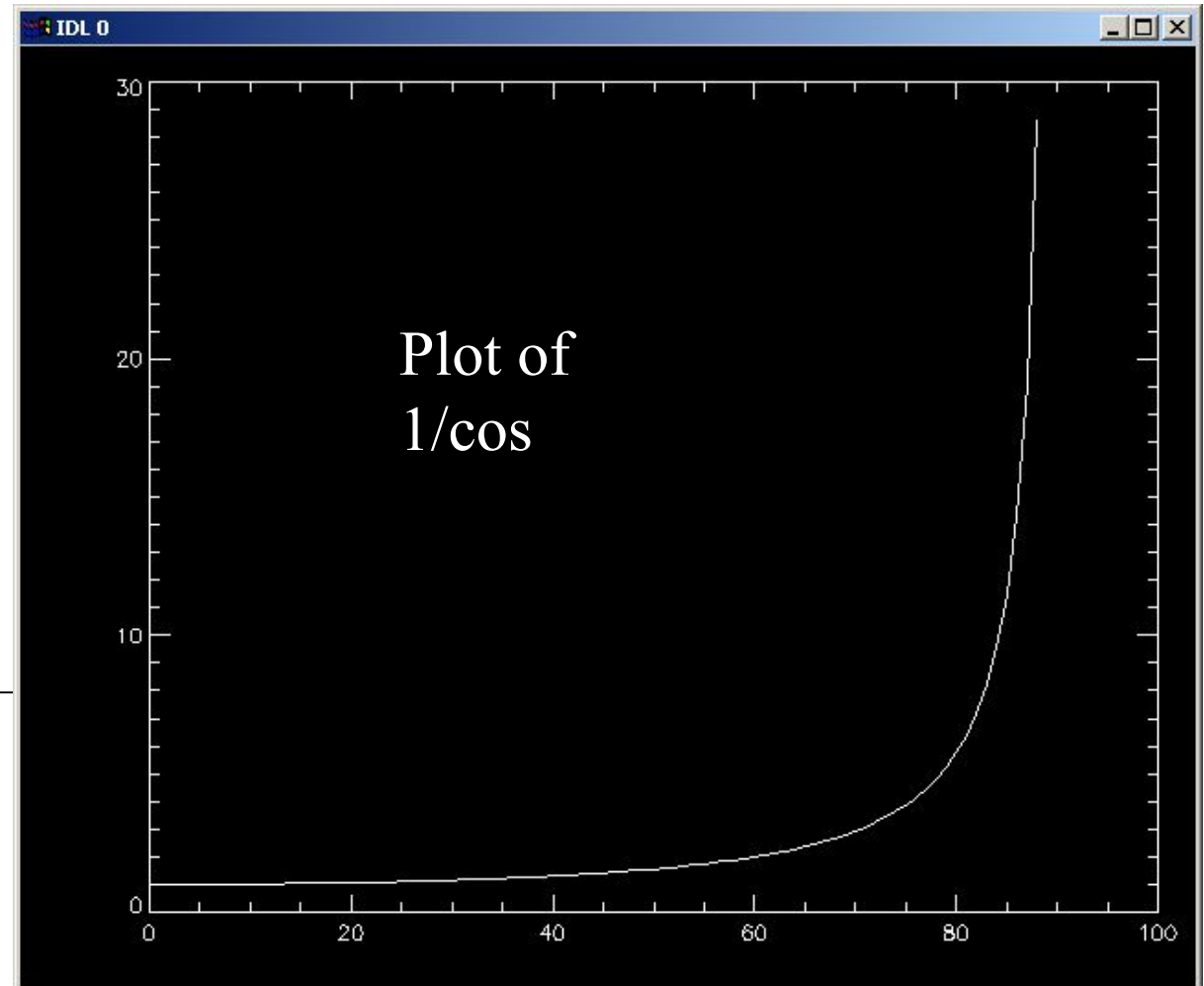
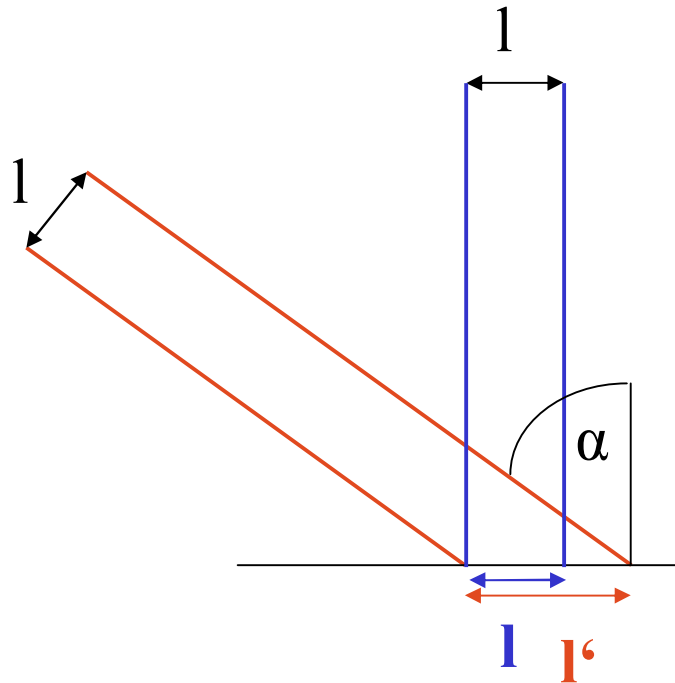
$$\text{Area } A' = A_{90^\circ} / \cos \alpha$$

Radiant Flux [W m^{-2}]

$$E_\alpha = E_0 \cos \alpha$$

Physical Basics

Lambertian Cos.-Law

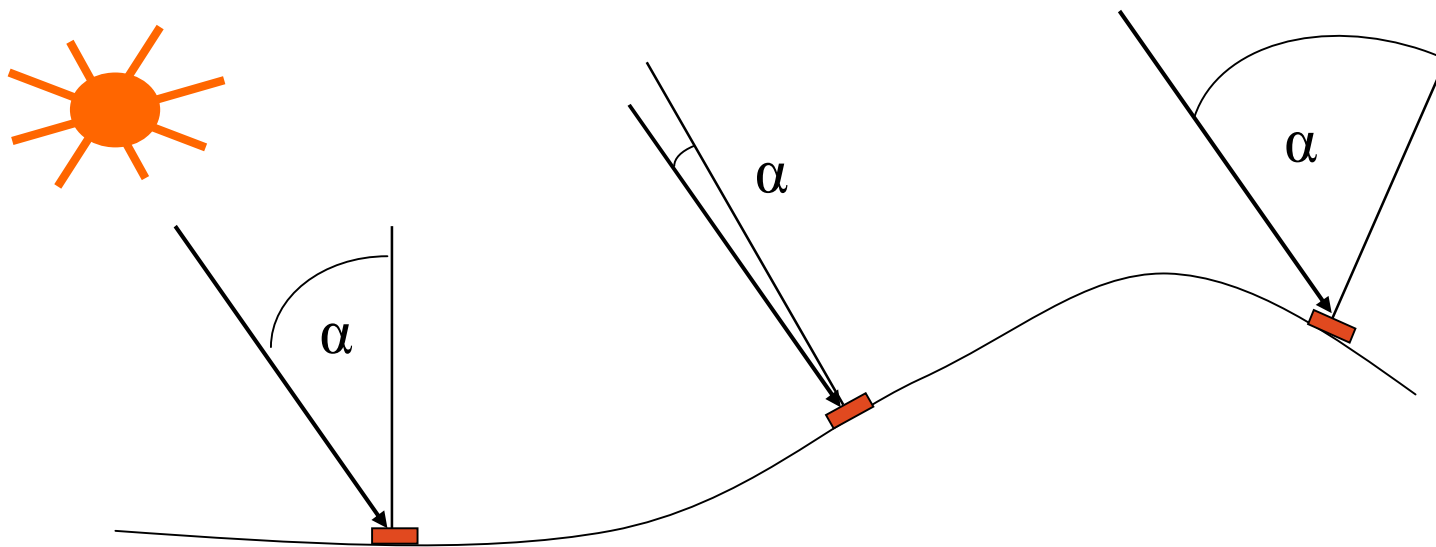


Physical basics

Radiant Flux [W m^{-2}]

$$E_{\alpha} = E_0 \cos \alpha$$

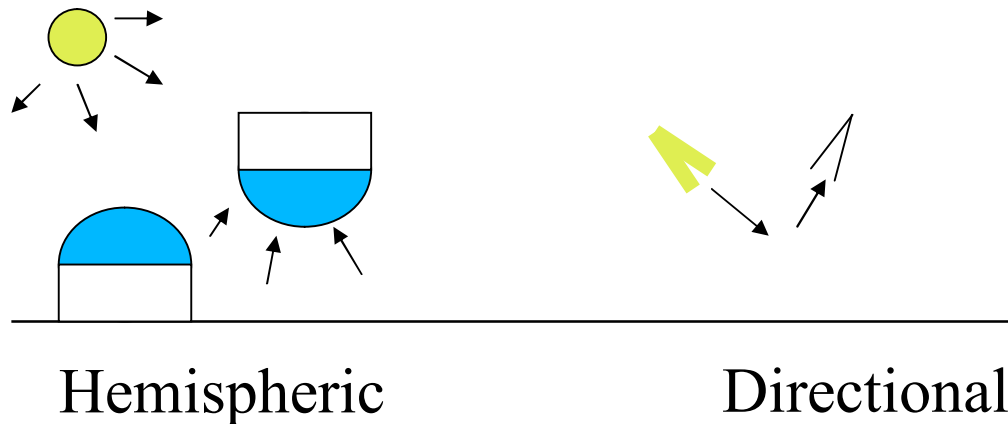
=> Illumination condition depends on relief & sun angle




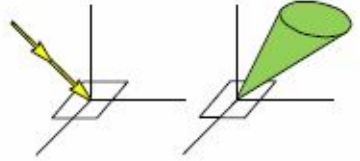
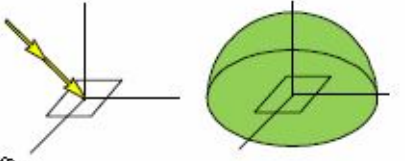
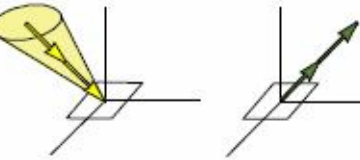
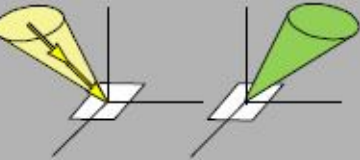
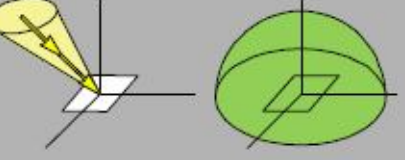
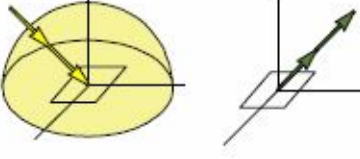
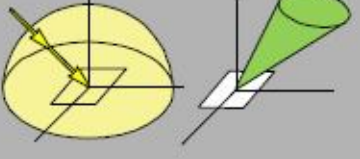
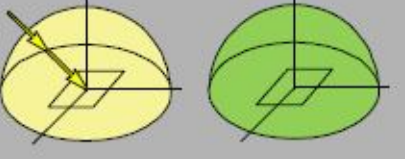
... Reflectance Nomenclature:

Physical Basics

- Bidirectional
directional illumination, observation in one direction
- Directional - hemispheric
directional illumination, observation of hemisphere
- Hemispheric - directional
hemispherical illumination, observation in one direction
- Hemispheric - hemispheric
hemispherical illumination, observation of hemisphere



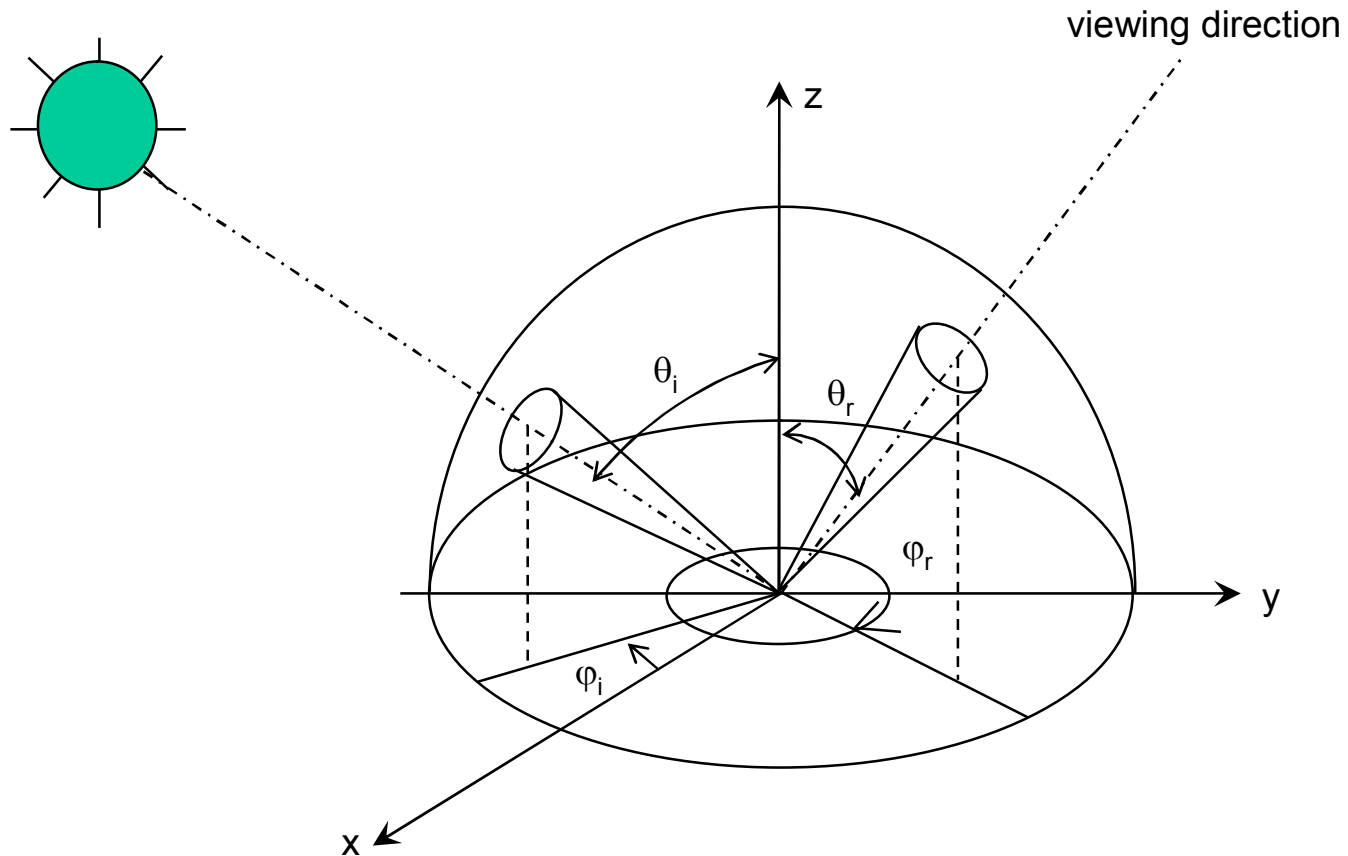
Physical Basics

<i>Incoming/Reflected</i>	Directional	Conical	Hemispherical
<i>Directional</i>	Bidirectional Case 1 	Directional-conical Case 2 	Directional-hemispherical Case 3 
<i>Conical</i>	Conical-directional Case 4 	Biconical Case 5 	Conical-hemispherical Case 6 
<i>Hemispherical</i>	Hemispherical-directional Case 7 	Hemispherical-conical Case 8 	Bihemispherical Case 9 

Physical Basics

BRDF

Bidirectional Reflectance Distribution Function



Physical Basics

- BRDF

$L_\lambda = \rho_\lambda E_\lambda (\cos \Theta) f_r$ $f_r =$ bidirectional reflectance distribution function
 for Lambertian surfaces.: $\rho_\lambda = (L \lambda \pi) / (E \lambda \cos \Theta)$

- Shade due to surface roughness
- HotSpot-effect:

If view direction = illumination direction \Rightarrow no shade visible

\Rightarrow brighter & specular \Rightarrow no Lambertian

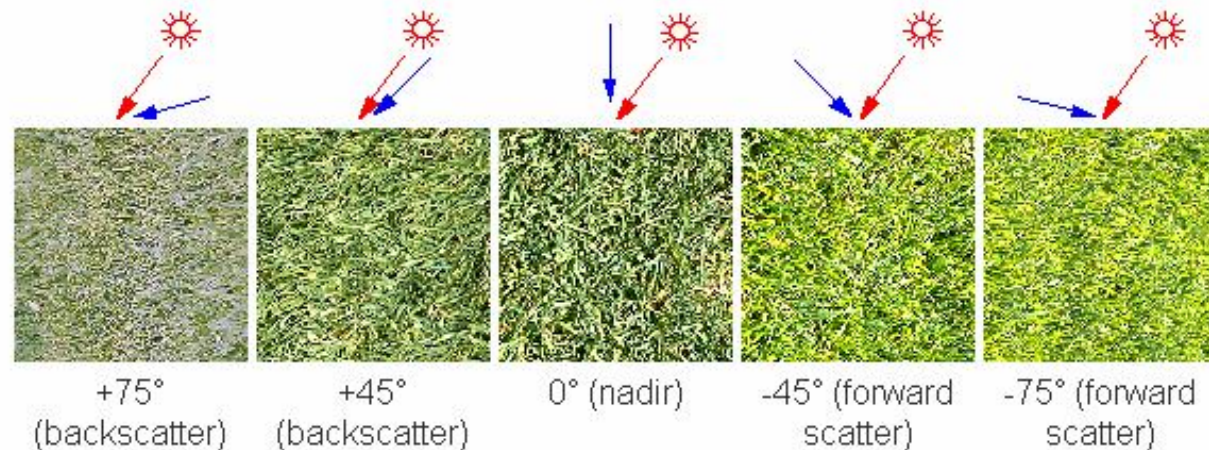


Fig. 2: Bidirectional reflectance effect on a grass lawn, observed under different viewing angles from a FIGOS mounted camera in the solar principal plane. Solar zenith angle is 35°, indicated with red arrows. The view directions are given in blue. The camera is operated in the manual modus keeping aperture, exposure time and focal length constant (k=16, t=1/15, f=135mm).